## Statewide Analysis: Spring 2009 CRCT Grades 1-8

Presented to the State Board of Education on February 10, 2010

## Rationale for this Investigation

The Governor's Office of Student Achievement is charged with auditing and inspecting schools and Local Education Agencies (O.C.G.A. § 20-12-24). A comprehensive analysis of the 2009 Spring CRCT data conducted by the state's vendor, СТВ McGraw-Hill, showed an unusually high number of answers changed from wrong to right (WTR) in some classrooms. Based on a conservative criterion for identifying unusual results, OSA makes the recommendations in this report to help eliminate test tampering and to help students adversely affected where applicable.

Because important decisions for individual students and for schools are based on CRCT data, it is vital that results indicate an accurate representation of students' knowledge.

## Purpose of the Criterion Referenced Competency Test (CRCT)

The CRCT is a standardized assessment administered to students in grades 1-8 in Georgia. It is designed to measure how well students at each grade level have acquired the knowledge and skills within the state's curriculum, the Georgia Performance Standards.

CRCT results are used to determine whether schools have made Adequate Yearly Progress (AYP) as required by the No Child Left Behind (NCLB) Act.

## Executive Summary

## Erasure Analysis

The state's test vendor for the CRCT, CTB-McGraw Hill, conducted an analysis of erasures on the answer sheets used in the spring 2009 CRCT. The analysis was conducted for grades 1-8, in Reading, Language Arts and Math and was designed to identify whether answers were changed from wrong to right more frequently in any classrooms compared to the rest of the state test population in each grade and subject.

Using a professional grade scanner, CTB scanned the answer documents to determine the total number of erasures and the total number of wrong-to-right (WTR) changes on each answer document. CTB then aggregated those results at the classroom level. Any classroom in which the number of WTR changes was 3 standard deviations (SD) or more (adjusted for class size) above the state average for that particular grade and subject was "flagged" as having an unusually high number of WTR changes. CTB aggregated these results at the school level.

## Erasure Analysis Results

The analysis indicates that some classrooms show an unusually high number of wrong answers changed to right answers on the grades 1-8 Spring 2009 CRCT in Reading, Language Arts and Math. At the school level, the percentage of classrooms flagged using the conservative criterion of 3 SD above the state average ranged from $0 \%$ to $89.5 \%$, with a statewide average of $4 \%$.

GOSA placed schools into four categories based on the percentage of classrooms within each school flagged according to CTB's results: Clear of concern; Minimal concern; Moderate concern; and Severe concern.
$80 \%$ of Georgia's elementary and middle schools fell into the "Clear" category, $10 \%$ fell into "Minimal concern," $6 \%$ fell into "Moderate concern," and 4\% fell into the "Severe concern" category.

## Erasure Analysis

## Submitted by CTB-McGraw Hill

January 22, 2010

With the high-stakes nature of large-scale assessments such as the CRCT, there are times when student's responses, and hence their scores, may not be a true representation of their own abilities. Various activities may take place, such as a student copying from another student's paper, students receiving inappropriate assistance before or during testing, or students' responses altered after testing. To maintain the integrity of the CRCT and the validity of the results, it is important that any such instances be discovered.

The present study investigated student responses on the Reading, English Language Arts, and Mathematics Spring 2009 CRCT that a) were erased and b) changed from wrong to right answers

Reviewers should note that results should only be used to facilitate identification of systematic problems within individual schools. That is, these types of analyses must be supported by additional, collateral information.

## Method

The basis for the erasure analysis is to count erasures in items where an answer choice was erased and replaced with another answer choice. Often the data captured is useful for identifying cases of cheating. During erasure analysis, two sets of erasures were analyzed: all erasures and wrong-toright erasures where an incorrect answer choice was erased and replaced with the correct answer choice. Please note that, for the erasure analyses, all items (either the operational or field-test) were included, as field test items were all embedded in CRCT.

The basic idea underlying the procedure is a statistical test of the null hypothesis $\left(\mathrm{H}_{0}\right)$ that the mean number of erasures for a class constitutes a random sample from the state distribution of erasures. The hypothesis is tested against the (right-sided) alternative $\left(\mathrm{H}_{1}\right)$ that the mean number is too high to be explained by random sampling. Classes for which $\mathrm{H}_{0}$ has to be rejected are flagged for further scrutiny. A well-known central limit theorem in statistics tells us that the sampling distribution of mean number of erasures for class $i\left(m_{i}\right)$ is asymptotically normal with mean and standard deviation

$$
\begin{align*}
& \operatorname{Mean}\left(m_{i}\right)=\mu  \tag{1}\\
& \operatorname{SD}\left(m_{i}\right)=\frac{\sigma}{\sqrt{n_{i}}} \tag{2}
\end{align*}
$$

where $n_{i}$ and $m_{i}$ denote the size and mean number of erasures for class $i$, respectively. In addition, $\mu$ and $\sigma$ denote the mean and the standard deviation of the distribution of the number of erasures of the population of individual students in the state of Georgia.

It is evident in the formula for the state standard deviation that the class flagging criterion for each class is adjusted for the number of test takers in a classroom. For example, if the state mean and SD of erasure count are 1.73 and 2.11 , respectively, the flagging criterion for a class size of 20 is adjusted to $3.15\left(1.73+3 \frac{2.11}{\sqrt{20}}=3.15\right)$.

This adjustment ensures that the flagging criterion is equally stringent for classes with considerably different numbers of test takers. In addition, minimizing the probability of false positive (Type I) errors in this statistical test is crucial in this analysis.

The classes were flagged if their $m_{i}$ was larger than $\mu+3 \frac{\sigma}{\sqrt{n_{i}}}$. Statistically, the flagging criterion set at or above $3 \sigma$ is conservative. The standard normal table shows that under random sampling the (asymptotic) probability of a sample mean being more than three standard deviations above the population mean is around 0.001 . However, rejection of $H_{0}$ only tells us that the observed mean number of erasures is unlikely to be the result of random sampling.

## Results

Table A. 1 reports the state summary for erasure counts. The mean number of erasures across grades and subjects ranged from 1.40 to 3.07 for the 2009 spring CRCT. The erasure count at the $95^{\text {th }}$ percentile point was between 5 and 9 . Table A. 2 reports the state summary for wrong-to-right erasure counts. As can be expected, the mean wrong-to-right erasure count and the count at the $95^{\text {th }}$ percentile point were lower than those obtained from all erasure counts. The mean number of wrong-to-right erasures ranged from 0.81 to 1.91 for the 2009 spring CRCT. The wrong-to-right erasure count at the $95^{\text {th }}$ percentile point was between 3 and 6 .

Table 1 summarizes all erasure analyses and wrong-to-right erasure analyses. Table 1 presents the number of schools flagged across three content areas -Reading, English/Language Arts, and Mathematics - within each analysis of spring CRCT. For each analysis, the number of schools was computed in two ways: flagged for at least one content area or flagged for all three content areas.

Separate reports were produced displaying the results of all erasure analyses and wrong-to-right erasure analyses. The number/percentage of schools that had zero flags for all erasures and wrong-to-right erasures in Reading, English/Language Arts, and Mathematics and is provided in Table 2.

The number/percentage of schools that had less than 1\% of classes flagged for all erasures and wrong-to-right erasures in Reading, English/Language Arts, and Mathematics and across grades is provided in Table 3.

Table 1. The number of schools flagged across three content areas

| Grade | Total <br> Number of <br> Schools | All Erasure Analyses <br> Schools Flagged <br> for at Least One <br> Content Area | Number of <br> Schools Flagged <br> for All Content <br> Areas | Wrong-to-Right Erasure Analyses <br> Schools Flagged of <br> for at Least One <br> Content Area  Number of <br> Schools Flagged <br> for All Content <br> Areas <br> 1  $\quad 1228$ | 478 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 180 |  |  |  |
| 2 | 1230 | 424 | 174 | 392 | 161 |
| 3 | 1232 | 368 | 94 | 316 | 80 |
| 4 | 1233 | 298 | 68 | 250 | 50 |
| 5 | 1235 | 316 | 90 | 252 | 69 |
| 6 | 591 | 220 | 45 | 154 | 23 |
| 7 | 567 | 204 | 55 | 148 | 23 |
| 8 | 566 | 220 | 65 | 156 | 39 |

Table 2. The number and percentage of schools that had zero flags for all erasures and wrong-toright erasures (Spring CRCT)

| Grad e | Reading |  |  | English/Language Arts |  |  | Mathematics |  |  | Reading, <br> English/Language Arts, and Mathematics |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | No. of School s | No. of School <br> s with <br> zero <br> flags | \% of School $s$ with zero flags | No. of School s | No. of School <br> $s$ with zero flags | \% of School $s$ with zero flags | No. of School $s$ | No. of School <br> $s$ with zero flags | \% of School s with zero flags | No. of School s | No. of School <br> $s$ with zero flags | \% of School $s$ with zero flags |
| 1 | 1226 | 852 | 69\% | 1226 | 880 | 72\% | 1226 | 845 | 69\% | 1226 | 700 | 57\% |
| 2 | 1229 | 909 | 74\% | 1229 | 914 | 74\% | 1229 | 903 | 73\% | 1229 | 771 | 63\% |
| 3 | 1231 | 969 | 79\% | 1231 | 994 | 81\% | 1231 | 1014 | 82\% | 1231 | 816 | 66\% |
| 4 | 1231 | 1036 | 84\% | 1231 | 1019 | 83\% | 1230 | 1063 | 86\% | 1231 | 884 | 72\% |
| 5 | 1233 | 1019 | 83\% | 1232 | 1007 | 82\% | 1233 | 1057 | 86\% | 1233 | 879 | 71\% |
| 6 | 590 | 436 | 74\% | 589 | 438 | 74\% | 589 | 484 | 82\% | 590 | 350 | 59\% |
| 7 | 566 | 414 | 73\% | 566 | 434 | 77\% | 566 | 449 | 79\% | 566 | 341 | 60\% |
| 8 | 564 | 401 | 71\% | 564 | 409 | 73\% | 564 | 450 | 80\% | 564 | 330 | 59\% |

Table 3. The number and percentage of schools that had less than $1 \%$ of classes flagged for all erasures and wrong-to-right erasures across grades

| Reading |  |  | English/Language Arts |  |  | Mathematics |  |  | Reading, English/Language Arts, and Mathematics |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Schools | No. of School <br> s with <1\% flags across grades | No. of School s with <1\% flags across grades | No. of Schools | No. of School <br> s with <1\% flags across grades | No. of School <br> s with <1\% flags across grades | No. of Schools | No. of School s with <1\% flags across grades | No. of School s with <1\% flags across grades | No. of Schools | No. of School s with <1\% flags across grades | No. of School s with <1\% flags across grades |
| 1857 | 1191 | 64\% | 1857 | 1220 | 66\% | 1857 | 1260 | 68\% | 1857 | 1594 | 86\% |

## Discussion

With respect to the erasure analyses, the following caveats are always applicable:

1. The normal distribution holds only for large classes; for smaller classes the result is approximate.
2. Rejection of $\mathrm{H}_{0}$ does not necessarily imply cheating. Alternative explanations are possible.
3. The flagging criterion should thus be taken as a stimulus to look for additional evidence and find out what happened in the school.

This erasure analysis is considered a check for unusual numbers of erasures to student responses. Without additional layers added to the analysis, this kind of check only addresses the possibility, not the certainty, of teachers or administrators altering the responses of students.

Appendix

## Scanning Operations Documentation

## CTB-McGraw Hill

With the high-stakes nature of large-scale assessments such as the CRCT, there are times when student's responses, and hence their scores, may not be a true representation of their own abilities. Various activities may take place, such as a student copying from another student's paper, students receiving inappropriate assistance before or during testing, or students' responses altered after testing. To maintain the integrity of the CRCT and the validity of the results, it is important that any such instances be discovered.

This memorandum is designed to provide some additional documentation in support of a research study that investigated student responses on the Reading, English Language Arts, and Mathematics Spring 2009 CRCT that a) were erased and b) changed from wrong to right. Specifically, it provides information regarding the scanning operations as they pertain to erasure analyses and associated quality control checks.

It should be emphasized that results from erasure analyses performed in 2009 should only be used to identify potential problems within individual classrooms. That is, these types of analyses must be supported by additional investigations and collateral information before conclusions regarding any improprieties are reached.

## Scanning Operations

The GA CRCT answer documents were processed using high speed 5000i optical scanners which reliably capture document images and optical mark read data. The sophisticated proprietary scoring software system WinScore reviews the integrity of each batch of documents scanned according to pre-defined guidelines and services. This flexible system reduces scanning/scoring time and provides a high degree of quality control.

The WinScore system provides a mechanism for identifying multiple-marks and identification of erasures for scanned data. The basis of the erasure analysis is to count erasures for multiple choice items where two or more responses have been made with specified intensity. Erasure analyses provide a mechanism to differentiate between three kinds of answer changes: a) wrong-to-wrong, b) right-to-wrong and c) wrong-to-right. Capturing the frequency of answer changes from wrong to right can be useful for identifying potential instances of cheating at the student level. Erasure analyses results can be grouped to tentatively identify problems at the classroom and school levels.

An erasure analysis involves an analysis of scanner data where additional marks have been made on student answer documents. As part of our quality control check for the 2009 CRCT erasure analyses, we pulled 19487 student papers from 17 schools - and checked whether the wrong-to-right erasures could be confirmed. Over $96 \%$ of answer changes were confirmed by raters. The remaining $4 \%$ of answer changes were likely due to unintended marks on answer documents made and were distributed throughout the 20K papers examined. This extensive review of the CRCT answer changes indicates that the scanning software employed in the erasure analysis accurately identified students changing wrong to right answers.

Table A.1. State summary for all types of erasure counts

| Content | Grade | N_state | ERA_state | Mean_state | Std_state | Min_state | Max_state | P10_state | P25_state | P50_state | P75_state | P90_state | P95_state |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| RD | 1 | 128,257 | 221,495 | 1.73 | 2.11 | 0 | 31 | 0 | 0 | 1 | 3 | 4 | 6 |
|  | 2 | 129,365 | 181,429 | 1.40 | 1.87 | 0 | 40 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 3 | 128,837 | 251,810 | 1.95 | 2.70 | 0 | 44 | 0 | 0 | 1 | 3 | 5 | 7 |
|  | 4 | 125,267 | 212,860 | 1.70 | 2.44 | 0 | 50 | 0 | 0 | 1 | 2 | 4 | 6 |
|  | 5 | 124,798 | 251,418 | 2.01 | 2.71 | 0 | 43 | 0 | 0 | 1 | 3 | 5 | 7 |
|  | 6 | 120,336 | 174,097 | 1.45 | 2.04 | 0 | 49 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 7 | 120,692 | 168,982 | 1.40 | 1.98 | 0 | 41 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 8 | 120,859 | 188,964 | 1.56 | 2.12 | 0 | 41 | 0 | 0 | 1 | 2 | 4 | 5 |
| LA | 1 | 128,226 | 306,476 | 2.39 | 2.65 | 0 | 34 | 0 | 1 | 2 | 3 | 6 | 7 |
|  | 2 | 129,328 | 259,145 | 2.00 | 2.37 | 0 | 50 | 0 | 0 | 1 | 3 | 5 | 6 |
|  | 3 | 128,767 | 301,406 | 2.34 | 2.85 | 0 | 55 | 0 | 0 | 2 | 3 | 6 | 8 |
|  | 4 | 125,239 | 276,556 | 2.21 | 2.83 | 0 | 60 | 0 | 0 | 1 | 3 | 5 | 7 |
|  | 5 | 124,744 | 285,415 | 2.29 | 2.85 | 0 | 53 | 0 | 0 | 1 | 3 | 5 | 7 |
|  | 6 | 120,283 | 191,496 | 1.59 | 2.29 | 0 | 56 | 0 | 0 | 1 | 2 | 4 | 6 |
|  | 7 | 120,629 | 173,625 | 1.44 | 2.10 | 0 | 49 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 8 | 120,724 | 203,763 | 1.69 | 2.35 | 0 | 52 | 0 | 0 | 1 | 2 | 4 | 6 |
| MA | 1 | 128,434 | 321,641 | 2.50 | 2.70 | 0 | 40 | 0 | 1 | 2 | 4 | 6 | 8 |
|  | 2 | 129,540 | 328,724 | 2.54 | 2.72 | 0 | 61 | 0 | 1 | 2 | 4 | 6 | 8 |
|  | 3 | 129,046 | 367,994 | 2.85 | 3.25 | 0 | 57 | 0 | 1 | 2 | 4 | 7 | 9 |
|  | 4 | 125,470 | 368,661 | 2.94 | 3.39 | 0 | 68 | 0 | 1 | 2 | 4 | 7 | 9 |
|  | 5 | 125,019 | 368,460 | 2.95 | 3.48 | 0 | 60 | 0 | 1 | 2 | 4 | 7 | 9 |
|  | 6 | 120,478 | 308,007 | 2.56 | 2.96 | 0 | 67 | 0 | 1 | 2 | 4 | 6 | 8 |
|  | 7 | 120,777 | 249,930 | 2.07 | 2.62 | 0 | 54 | 0 | 0 | 1 | 3 | 5 | 7 |
|  | 8 | 120,953 | 342,054 | 2.83 | 3.33 | 0 | 66 | 0 | 1 | 2 | 4 | 7 | 9 |

Table A.2. State summary for wrong-to-right (WTR) erasure count

| Content | Grade | N_state | WTR_state | Mean_state | Std_state | Min_state | Max_state | P10_state | P25_state | P50_state | P75_state | P90_state | P95_state |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| RD | 1 | 128,257 | 138,593 | 1.08 | 1.49 | 0 | 23 | 0 | 0 | 1 | 2 | 3 | 4 |
|  | 2 | 129,365 | 118,288 | 0.91 | 1.38 | 0 | 28 | 0 | 0 | 0 | 1 | 2 | 3 |
|  | 3 | 128,837 | 151,060 | 1.17 | 1.87 | 0 | 35 | 0 | 0 | 1 | 2 | 3 | 4 |
|  | 4 | 125,267 | 124,590 | 0.99 | 1.64 | 0 | 36 | 0 | 0 | 0 | 1 | 3 | 4 |
|  | 5 | 124,798 | 141,789 | 1.14 | 1.83 | 0 | 37 | 0 | 0 | 1 | 2 | 3 | 4 |
|  | 6 | 120,336 | 98,587 | 0.82 | 1.30 | 0 | 29 | 0 | 0 | 0 | 1 | 2 | 3 |
|  | 7 | 120,692 | 97,579 | 0.81 | 1.27 | 0 | 33 | 0 | 0 | 0 | 1 | 2 | 3 |
|  | 8 | 120,859 | 111,596 | 0.92 | 1.39 | 0 | 35 | 0 | 0 | 1 | 1 | 2 | 3 |
| LA | 1 | 128,226 | 205,551 | 1.60 | 1.95 | 0 | 30 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 2 | 129,328 | 170,610 | 1.32 | 1.73 | 0 | 43 | 0 | 0 | 1 | 2 | 3 | 4 |
|  | 3 | 128,767 | 194,150 | 1.51 | 2.05 | 0 | 37 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 4 | 125,239 | 175,974 | 1.41 | 2.03 | 0 | 41 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 5 | 124,744 | 178,967 | 1.43 | 2.04 | 0 | 34 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 6 | 120,283 | 115,767 | 0.96 | 1.55 | 0 | 36 | 0 | 0 | 0 | 1 | 3 | 4 |
|  | 7 | 120,629 | 110,213 | 0.91 | 1.48 | 0 | 41 | 0 | 0 | 0 | 1 | 3 | 4 |
|  | 8 | 120,724 | 125,520 | 1.04 | 1.63 | 0 | 41 | 0 | 0 | 1 | 1 | 3 | 4 |
| MA | 1 | 128,434 | 224,507 | 1.75 | 2.05 | 0 | 30 | 0 | 0 | 1 | 3 | 4 | 6 |
|  | 2 | 129,540 | 223,945 | 1.73 | 2.05 | 0 | 44 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 3 | 129,046 | 241,822 | 1.87 | 2.43 | 0 | 41 | 0 | 0 | 1 | 3 | 5 | 6 |
|  | 4 | 125,470 | 235,186 | 1.87 | 2.44 | 0 | 47 | 0 | 0 | 1 | 3 | 5 | 6 |
|  | 5 | 125,019 | 228,146 | 1.82 | 2.54 | 0 | 45 | 0 | 0 | 1 | 2 | 4 | 6 |
|  | 6 | 120,478 | 171,897 | 1.43 | 1.96 | 0 | 43 | 0 | 0 | 1 | 2 | 4 | 5 |
|  | 7 | 120,777 | 143,487 | 1.19 | 1.77 | 0 | 41 | 0 | 0 | 1 | 2 | 3 | 4 |
|  | 8 | 120,953 | 186,083 | 1.54 | 2.14 | 0 | 45 | 0 | 0 | 1 | 2 | 4 | 5 |

## Formal Recommendations that Require Action by the State Board of Education

Recommendations are intended to eliminate test tampering and help students who were adversely affected by intentional wrongdoing.

|  | State Action | LEA Corrective Action | LEA Student Support |
| :--- | :--- | :--- | :--- |
| $\begin{array}{l}\text { Severe Concern } \\ \text { classrooms flagged) }\end{array}$ | $\begin{array}{l}\text { State Monitors } \\ \text { during Spring } \\ 2010 \text { CRCT }\end{array}$ | $\begin{array}{l}\text { 1) LEA to conduct an } \\ \text { investigation } \\ \text { 2) Submit results of } \\ \text { investigation to OSA } \\ \text { 3) Rotate teachers during } \\ \text { CRCT. }\end{array}$ | $\begin{array}{l}\text { 1) Notify parents } \\ \text { 2) Offer student }\end{array}$ |
| support services as |  |  |  |
| appropriate based on |  |  |  |
| outcomes of LEA |  |  |  |
| investigation |  |  |  |$]$| Moderate Concern |
| :--- |
| (11\%-24\% of <br> classrooms flagged) |
| Random Spot <br> Checks by State <br> Monitors |
| 1) LEA to conduct an <br> investigation <br> 2) Submit results of <br> investigation to OSA <br> 3) Rotate teachers during <br> CRCT. <br> 4) Monitor test environment. |
| Minimal Concern <br> (6\%-10\% of classrooms <br> flagged) |

